

Damage Mechanism of Drift Ice Impact

Li Gong*, Zhonghui Wang*, Yaxian Li*, Chunling Jin*, and Jing Wang*

Abstract

The ice damage occurs frequently in cold and dry region of western China in winter ice period and spring thaw period. In the drift ice condition, it is easy to form different extrusion force or impact force to damage tunnel lining, causing project failure. The failure project could not arrive the original planning and construction goal, giving rise to the water allocation pressure which influences diversion irrigation and farming production in spring. This study conducts the theoretical study on contact-impact algorithm of drift ices crashing diversion tunnel based on the symmetric penalty function in finite element theory. ANSYS/LS-DYNA is adopted as the platform to establish tunnel model and drift ice model. LS-DYNA SOLVER is used as the solver and LS-PREPOST is used to do post-processing, analyzing the damage degrees of drift ices on tunnel. Constructing physical model in the experiment to verify and reveal the impact damage mechanism of drift ices on diversion tunnel. The software simulation results and the experiment results show that tunnel lining surface will form varying degree deformation and failure when drift ices crash tunnel lining on different velocity, different plan size and different thickness of drift ice. The researches also show that there are damages of drift ice impact force on tunnel lining in the thawing period in cold and dry region. By long time water scouring, the tunnel lining surfaces are broken and falling off which breaks the strength and stability of the structure.

Keywords

Damage Mechanism, Drift Ice, Impact

1. Introduction

Northwest China is located in the high, dry and cold region whose temperature is low and drift ice season is long in winter. Meanwhile, there is serious water shortage in this region, especially in part of Gansu Province, even the drinking water is in short supply. In order to ease the severe water shortage situation, the country successively invests and constructs a large numbers of water diversion projects for drinking and farm irrigation, such as the Datong River to Qinwangchuan region water diversion project, Tao River water diversion project, and so on. And the prepared west line of South-to-North [1] water diversion project is unprecedented. In winter operation period, the drift ice or ice berg would occur in the diversion projects under low temperature. They may cause serious impacts on water diversion project, including the influence of ice cover and ice berg on diversion capacity, the impact of ice expansion force on channel, the damage of drift ice on diversion tunnel, the impact of ice on channel operation and project security, and so on.

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Manuscript received September 11, 2019; accepted October 21, 2019.

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Domestic and foreign scholars have studied the evolution of ice conditions during the icing period, Domestic scholar Wang et al. [2] have conducted experimental research on the accumulation process of ice plugs by means of a sink test, Zhao et al. [3] conducted a study on the formation process of the ice and the formation of the ice in the Shensifenzi Bend, Wang et al. [4] introduced the influence of thermodynamic processes on the simulation of the sea ice and the elimination of the sea, and Shi et al. [5] based on the ice creep test, a nonlinear Burgers' sea ice model considering damage failure was established. The foreign scholar Jimenez et al. [6] established an updated-Lagrangian damage mechanics formulation for modeling the creeping flow and fracture of ice sheets, Marchenko and Cole [7] compared wave energy dissipation caused by three physical processes, Shortt and Sammonds [8] established the empirical scaling relations for sea ice mechanics by studying the micromechanics of ice. Jin et al. [9] proposed a gray GMP-Verhulst combination forecasting model identifies the change law of risk fluctuation. Gong et al. [10] used the symmetric penalty function in the finite element contact-impact algorithm to conduct the theoretical study on collision simulation problem between drift ice and water diversion tunnel.

In order to research the drift ice impact on the diversion tunnel in thawing period in long distance diversion project in cold and dry region, this study adopted theoretical analysis, numerical modelling and test research method. It intensively researched the impact force of the interaction between drift ice and diversion tunnel lining, using theoretical analysis, numerical simulation and testing research methods. The software of ANSYS/LS-DYNA was adopted as the platform to establish finite element model when the drift ice crashing diversion tunnel. The unilateralism slope experimental facility was also built to simulate evolution processes of drift ice crashing diversion tunnel. They reveal the impact influence regularity of drift ice on diversion tunnel on different working conditions. This study supplies theoretical support and technical guarantee for water conveyance project security in cold and dry region of western China.

2. Materials and Methods

2.1 Data Simulation of Drift Ice Impacting Diversion Tunnel

The control equations that describe the nonlinear motion, deformation and impact problem fall into two categories: Lagrange method and Euler method. This study adopts Lagrange method to solve contact-impact problem. In the Lagrange method, the quality of particle must remain unchanged during the particle moves with the object.

Particles move in the overall motion system must follow the basic flow equation which satisfies the energy, mass and momentum conservation governing equation. In this study, the basic equations of drift ice impacting tunnel lining are shown as follows.

2.1.1 Mass conservation equation

$$\rho(X,t)J(X,t) = \rho_0(X,0) \quad (1)$$

where $\rho_0(X,0)$ is the medium density of the initial model ($t=0$). $J(X,t)$ is the Jacobin determinate of the model.

2.1.2 Momentum conservation equation

$$\frac{\partial \sigma_{ij}}{\partial x_j} + \rho b_i = \rho \ddot{u}_i \quad (2)$$

where σ_{ij} is the current architectonic stress tensor. b_i is the acting force on the unit mass of drift ice model and tunnel model. \ddot{u}_i is the particles acceleration of the drift ice and tunnel model which is calculated by Eq. (3):

$$\ddot{u}_i = \frac{\partial^2 u_i(X, t)}{\partial t^2} = \frac{\partial^2 [x_i(X, t) - X_i]}{\partial t^2} = \frac{\partial^2 v_i(X, t)}{\partial t^2} \quad (3)$$

where $v_i(X, t)$ denotes the instantaneous velocity of the particle in time t and the coordinate of the particle is X .

2.1.3 Energy conservation equation

$$\rho \dot{w}^{\text{int}} = D_{ij} \sigma_{ij} \quad (4)$$

where \dot{w}^{int} is the derivation of internal energy of the drift ice and tunnel model with response to time. D_{ij} is the strain rate tensor which is calculated by Eq. (5).

$$D_{ij} = \frac{1}{2} \left(\frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right) \quad (5)$$

where v_i is the instantaneous velocity (m/s) of the particle in direction x . v_j is the instantaneous velocity (m/s) of the particle in direction y .

2.1.4 Boundary condition

The tunnel model current architectonic surface force boundary condition is

$$t_i = n_j \sigma_{ij} \quad (6)$$

where, t_i is the stress vector on surface element, n_j is the current architectonic directed surface element, and σ_{ij} is the stress vector of the current architectonic. The calculation requires the relative motion between drift ice and tunnel satisfies momentum conservation equation in the whole solution range. But in the practical engineering project, it is almost impossible to solute the results directly. In order to solve this problem, we introduced the numerical computation method which considers the weak form of the differential equation. It could get the momentum equation only by the inner product and further deduce the virtual power theory equations of the model. After the finite element discretization, the joint displacement equation of model is obtained.

Based on the weighted residual method in which virtual velocity is chosen as weighting coefficient, the weak form of the momentum equation is obtained. It is

$$\int_V \delta v_i \left(\frac{\partial \sigma_{ij}}{\partial x_j} + \rho b_i - \rho \ddot{u}_i \right) dV = 0 \quad (7)$$

where $\delta v_i(X)$ is the virtual velocity which is solved by Eq. (8).

$$\delta v_i(X) \in R_0 \quad R_0 = \left\{ \delta v_i \mid \delta v_i \in C^0(X), \delta v_i \Big|_{A_i} = 0 \right\} \quad (8)$$

where, R_0 and C^0 are the vector and damping matrix in time 0, respectively, A_i is the boundary surface of the model. Based on subsection integral principle, the balance formula of the contact force can be expressed as follow:

$$\int_V \frac{\partial(\delta v_i)}{\partial x_j} \sigma_{ji} dV - \int_V \delta v_i \rho b_i dV - \int_{A_i} \delta v_i \bar{t}_i dA + \int_V \delta v_i \rho \ddot{u}_i dV = 0 \quad (9)$$

In this way, all particles velocity, acceleration, virtual velocity and strain rate could be expressed as the follow equation set:

$$\begin{cases} \dot{u}_i(X, t) = N_i(X) \dot{u}_{ii}(t) \\ \ddot{u}_i(X, t) = N_i(X) \ddot{u}_{ii}(t) \\ D_{ij} = \frac{1}{2} \left(\frac{\partial \dot{u}_i}{\partial x_j} + \frac{\partial \dot{u}_j}{\partial x_i} \right) = \frac{1}{2} \left(\dot{u}_{ii} \frac{\partial N_i}{\partial x_j} + \dot{u}_{jj} \frac{\partial N_j}{\partial x_i} \right) \\ \delta v_i(x) = N_i(x) \delta v_{ii} \end{cases} \quad (10)$$

Transform all the equations in the equation set (10) to matrix form and substitute them into virtual power formula (9) to get Eq. (11).

$$M \ddot{U} + f^{\text{int}} = f^{\text{ext}} \quad (11)$$

where, \ddot{U} denotes the system acceleration array, f^{int} denotes the system internal force array, f^{ext} denotes the system external force array, and M denotes the system mass array irrelevant to time. Their expressions are (12) to (14).

$$f^{\text{int}} = \int_V B^T \sigma dV \quad (12)$$

$$f^{\text{ext}} = \int_V N^T \rho b dV + \int_{A_i} N^T \bar{t} dA \quad (13)$$

$$M = \int_V \rho N^T N dV = \int_{V_0} \rho_0 N^T N dV_0 \quad (14)$$

Solve the above Eq. (14) to get the particle displacement u_i in the current time, then further obtained structure strain and stress at that moment.

2.2 Finite Element Modelling

2.2.1 Case study

In the case study, we chose 20 m in the No. 3 Pandaoling tunnel (CH62+959.78--78+682.934) to analyze the impact of the drift ice on the tunnel by finite element modelling method. Pandaoling tunnel is in the Datong River to Qinwangchuan region water diversion project in western China is 15.723 km in length, longitudinal slope of 1/1000, design flow of $Q = 29 \text{ m}^3/\text{s}$ and increasing flow of $Q = 34 \text{ m}^3/\text{s}$. It is pressureless diversion tunnel with mixed type lining. The first lining is made up of anchor arm, spay

concrete, reinforced mesh and steel arch. The secondary lining is cash-in-place concrete and reinforced concrete. The tunnel with 4.2 m clear width, 4.4 m clear height has arch walls and sections with antiarch baseboard. It has semicircle roof with 2.1 m radius and antiarch baseboard with 9.75 m radius. The fillet is added at the sidewall and antiarch baseboard connection, it is 0.404 m in height and 0.337m in length. The early tunnel support tunnel section is shown in Fig. 1. The tunnel model is shown in Fig. 2.

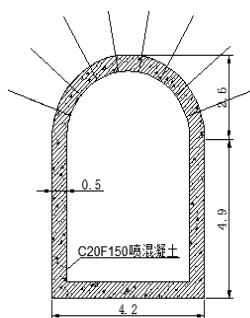


Fig. 1. Tunnel section primary support.

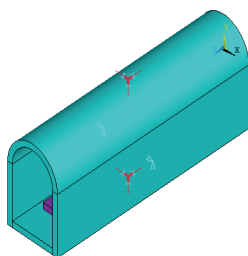


Fig. 2. Tunnel model diagram.

2.2.2 Project case study

ANSYS/LS-DYNA based on ALE and Euler algorithm has the functions of heat transfer analysis, fluid and solid coupling analysis, static analysis and implicit analysis. It could quickly solve the dynamic nonlinear problems of high velocity impact in plane or space, explosion, and so on. ANSYS/LS-DYNA was adopted to simulate the impact of drift ice on tunnel. The drift ice is floating on the water surface. So it just need consider the horizontal loads such as wind drag force and flow drag force, while ignoring vertical loads such as gravity, buoyancy force, and so on. The parameters of tunnel and drift ice are shown in Table 1. The horizontal load is mainly expressed by drift ice initial velocity. When the drift ice with different size and thickness impacts the tunnel surface with different velocity, the impact force is different. The impact force can be simulated by modelling.

Table 1. Physical property parameters of tunnel and drift ice

Elasticity modulus (Mpa)	Poisson ratio	Density (kg/m ³)	Compression strength (Mpa)	Tensile strength (Mpa)	Compressive strength (Mpa)
2.7×10 ¹⁰	0.3	2,500	-	-	-
8×10 ⁸	0.3	910	2.5	0.504	0.84

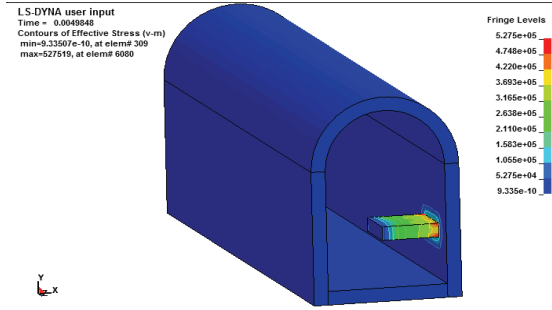


Fig. 5. Maximum impact force stress nephogram ($v = 0.5$ m/s).

2.3.1 Effect of drift ice velocity on impact force

The impact forces of drift ice crashing tunnel are different with different drift ice velocity. Set 2 m as water depth and $2 \times 0.5 \times 2$ m³ as drift ice size, and calculate the drift ice impact force when the drift ice velocities are 0.5, 0.8, 1.0, 1.5, 1.8, 2.0, 2.3, 2.5, 2.8, 3.0 m/s, respectively. Within the damage permissible limits, the calculation results of the drift ice impact force are shown in Fig. 5.

Different velocities produce different stress and impact force when the drift ice crashing the tunnel, the flow velocity-maximum stress relationship graph and flow velocity-maximum impact force relationship graph are shown in Fig. 6.

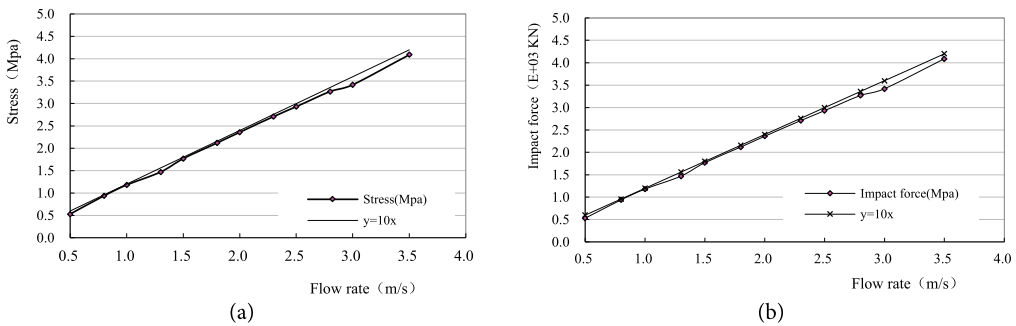


Fig. 6. (a) Flow velocity-maximum stress and (b) flow velocity-maximum impact force relational graph.

2.3.2 Effects of drift ice plane size on impact force

In order to research the influence of drift ice plane size on impact force, set 2 m as water depth, $v = 5$ m/s as drift ice velocity, 0.5 m as ice thickness. When the drift ice plane sizes are $0.5 \times 0.5 \times 2$ m³, $1.0 \times 0.5 \times 2$ m³, $1.5 \times 0.5 \times 2$ m³, $2 \times 0.5 \times 2$ m³, $2.5 \times 0.5 \times 2$ m³, which are 1, 2, 3, 4, 5 times of 0.5×0.5 m², respectively. Within the damage permissible limits, the calculation results of the drift ice impact force are shown in Fig. 7.

Different drift ice plane sizes produce different stresses and impact forces when drift ice crashing tunnel, the drift ice plane size-maximum stress relationship graph is shown in Fig. 8 and drift ice plane size-maximum impact force relationship is shown in Fig. 9.

Figs. 8 and 9 show that the collision stress relation curve is accordance with the collision impact force relation curve. When the drift ice has small plane size, the collision stress increases with the drift ice plane size, presenting linear relationship.

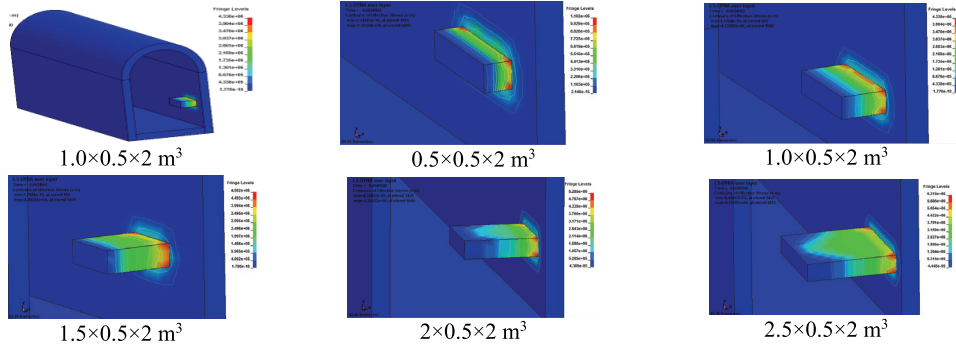


Fig. 7. Maximum impact force stress nephogram in different drift ice plan size.

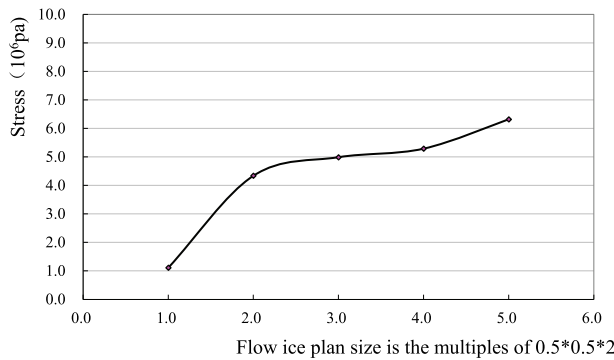


Fig. 8. Drift ice plan size-maximum stress relational graph.

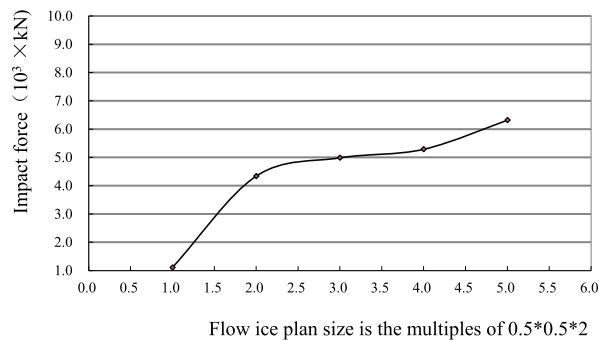


Fig. 9. Drift ice plan size-maximum impact force relational graph.

2.3.3 Effects of drift ice thickness on impact force

The drift ice thicknesses change, the impact force of drift ice crashing tunnel changes accordingly. When other parameters are fixed, and the drift ice thicknesses are 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0 m, respectively. Within the damage permissible limits, the calculation results of the drift ice impact force are shown in Fig. 10.

In different drift ice thicknesses, the relationship between maximum stress and thickness is shown in Fig. 11.

Fig. 12 shows that when other parameters are fixed, the impact force increases with the drift ice

thickness when the thickness is less than 0.9m, and the stress value has a little change when the thickness is larger than 0.9m. When the drift ice thickness is small, the impact force increases with the thickness, presenting approximate linear relationship.

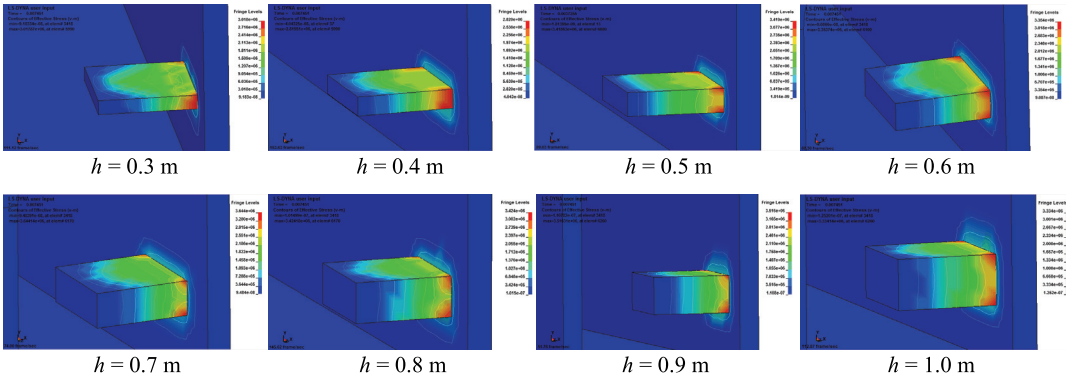


Fig. 10. Maximum impact force local stress nephogram in different drift ice thickness.

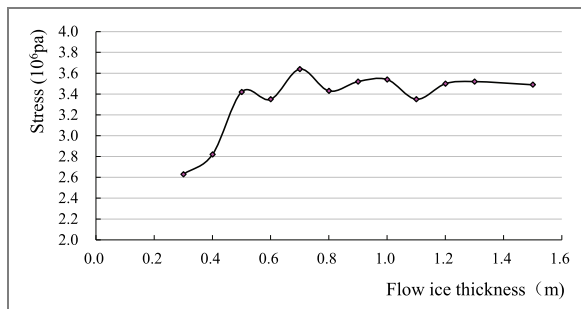


Fig. 11. Drift ice thickness-maximum stress relational graph.

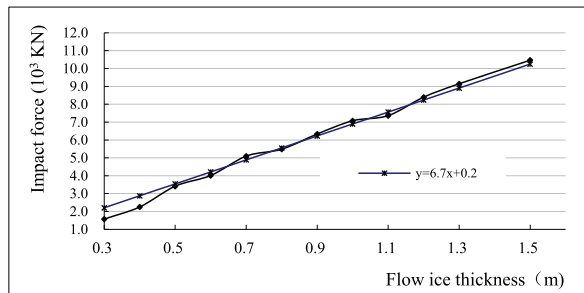


Fig. 12. Drift ice thickness-maximum impact force relational graph.

Above all, the tunnel lining surface would have different degrees of distortions when drift ice crashing tunnel lining in different drift ice velocity, different drift ice plane size, different drift ice thickness and so on. The distortions have little influence on the tunnel stability. But the tunnel lining surface breaks, and the tunnel lining surface would fall off by long time water erosion. It would destroy structure strength and stability. In the practical engineering, it would pay attention to this harm and adopt suitable protection measures.

2.4. Ice Mechanics Model Test

2.4.1 Test design

This study conducts indoor model test to research the impact mechanism of ice on tunnel in thawing period. In the indoor model test, the impact force of drift ice on diversion tunnel were tested on different drift ice plane size, different drift ice thickness, different drift ice velocity and so on. The model test state schematic diagram is shown in Fig. 13. Fig. 14 is the pump which used to pump water to other devices.

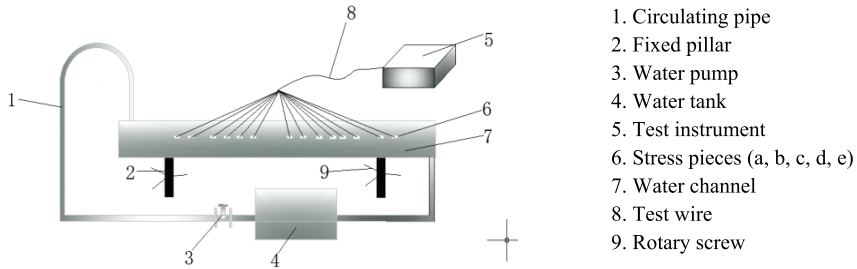


Fig. 13. Model test state schematic diagram.

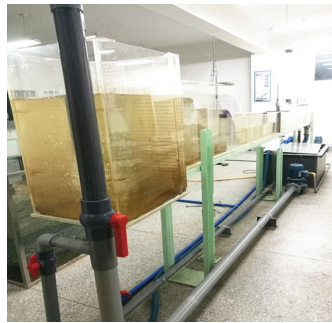


Fig. 14. The experimental device.



Fig. 15. Pump.

In this test, the main devices are a 2 m×1 m×1 m water tank which is used to store the water circulating in the system and a water pump which is the dominant body drives water from water tank to water channel, rises water level and operates circularly. They are shown in Fig. 15.

Test steps

The test has 15 steps:

Step 1: Fill the water tank with water.

Step 2: Open the main power and make water in the water tank rush into water channel by water pump.

Step 3: Put the ice blocks of 7 cm×3.5 cm×7 cm in water channel.

Step 4: Adjust flow velocity by rotary screw.

Step 5: The flow velocity is 0.5 m/s measured by flow meter.

Step 6: Measure the depth by water level probe and let the water depth be 7.2 cm.

Step 7: Stick 10 plexiglass strain gauges on the water line location of each side of tunnel model surface.

Step 8: Make the transient strain tester be close.

Step 9: Connect the strain gauges with transient strain tester by test wires and correspond each strain gauge with the joint in the transient strain tester.

Step 10: Turn on the transient strain tester and adjust to manual mode.

Step 11: Read the strain value which is the reading of the transient strain tester in sequence, along with the ice striking the tunnel surface.

Step 12: Record data, and process them.

Step 13: Change the conditions that set the flow velocity is 0.8, 1.0, 1.2, 1.5, 1.8, 2.0, 2.3, 2.5, 2.8, and 3.0 m/s, then repeat Step 4 to Step 12.

Step 14: Change the conditions that set the flow velocity is 1 m/s and set the ice blocks size to 7 cm×1 cm×7 cm, 7 cm×1.8 cm×7 cm, 7 cm×2.9 cm×7 cm, 7 cm×3.5 cm×7 cm, 7 cm×4.3cm×7 cm, 7 cm×5.5 cm×7 cm, respectively, then repeat Step 4 to Step 12.

Step 15: Change the conditions that set the flow velocity is 1 m/s and set the ice blocks size to 3.5 cm×1.8 cm×7 cm, 5.5 cm×1.8 cm×7 cm, 7 cm×1.8 cm×7 cm, 9 cm×1.8 cm×7 cm, respectively, then repeat Step 4 to Step 12.

3. Results

3.1 Effects of Flow Velocity on Impact Force

The drift ice velocity changes, the impact force and stress value on the tunnel surfaces changes accordingly, showing in Table 2.

Table 2. Tunnel side wall force values in different flow velocity

Flow rate v (m/s)	Model strain ε_m (E-05 KN)	Model stress σ_m (kPa)	Prototype stress σ_p (MPa)	Prototype impact force F_m (E+03 KN)
0.5	0.635793	21	0.6	0.6
0.8	0.794741	27	0.75	0.75
1	1.483520	50	1.4	1.4
1.3	1.769620	60	1.67	1.67
1.5	1.939170	65	1.83	1.83
1.8	2.543170	86	2.4	2.4
2	2.331240	79	2.2	2.2
2.3	2.755100	93	2.6	2.6
2.5	2.861070	96	2.7	2.7
2.8	3.178960	107	3	3
3	3.390890	114	3.2	3.2
3.5	4.026690	136	3.8	3.8

By analyzing large number of test data, it is found that the test results are close to the finite element simulation results. Fig. 16(a) shows that the impact force variations are approximately the same in the software simulation results, test observation calculation results and the results of $y = 10x$. Therefore, the finite element calculation method is feasible. The impact force of drift ice increases with the flow velocity, appearing linear distribution.

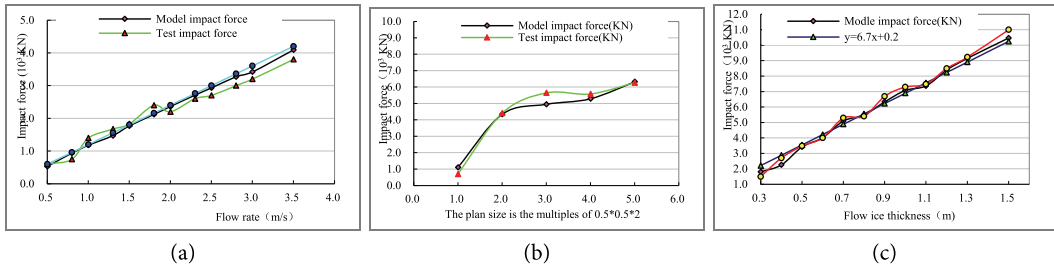


Fig. 16. Comparisons of test results and model simulation results: (a) flow velocity, (b) drift ice size, and (c) drift ice thickness on the impact force.

3.2 Effects of Drift Ice Size on the Impact Force

The drift ice sizes are different, the impact force and stress on tunnel surfaces are different. The values are shown in Table 3.

The comparison of test values and model simulation values are shown in Fig. 16(b). The test values are close to model simulation calculation values. The impact force increases with the drift ice size.

Table 3. Tunnel side wall force values in different drift ice plan size

Plan size	Model strain ε_m (E-05 KN)	Model stress σ_m (KPa)	Prototype stress σ_p (MPa)	Prototype impact force F_m (E+03 KN)
0.5×0.5×2	0.833333	25	0.7	0.7
1.0×0.5×2	5.250000	158	4.41	4.41
1.5×0.5×2	6.726190	202	5.65	5.65
2.0×0.5×2	6.642860	199	5.58	5.58
2.5×0.5×2	7.464290	224	6.27	6.27

3.3 Effects of Drift Ice Thickness on the Impact Force

By the tests, the drift ice thickness is different, the impact force and stress on the tunnel surfaces are different. The values are shown in Table 4.

The comparisons of test observation results and model calculation results are shown in Fig. 16(c). Fig. 16(c) shows that the impact force variations are approximately the same in the software simulation results, test observation calculation results and the results of $y = 6.7x + 0.2$. Therefore, the finite element calculation method is feasible. Within a certain range, the impact force of drift ice increases with the drift ice thickness, appearing linear distribution.

Table 4. Tunnel side wall force values in different drift ice thickness

Thickness (m)	Model strain ε_m (E-05 KN)	Model stress σ_m (kPa)	Prototype stress σ_p (MPa)	Prototype impact force F_m (E+03 KN)
0.3	2.64914	89	2500	1.5
0.4	3.57633	121	3375	2.7
0.5	3.6876	124	3480	3.48
0.6	3.53218	119	3333	4
0.7	4.01155	135	3786	5.3
0.8	3.57633	121	3375	5.4
0.9	3.94427	133	3722	6.7
1.0	3.86774	130	3650	7.3

4. Conclusions

The comparison results of software simulation and test observation show that their trends are almost the same. The impact force of drift ice on tunnel lining increases with the drift ice thickness, appearing linear distribution, which verifies the reliability of the following simulation results.

The researches show that there are damages of drift ice impact force on tunnel lining in the thawing period in cold and dry region. By long time water scouring, the tunnel lining surfaces are broken and falling off which breaks the strength and stability of the structure. With the increasing of the size, thickness and the flow velocity of the drift ice, the impact force is different.

In different ice velocity, different size, different thickness of the drift ice, the tunnel lining surfaces would be destroyed and deformed when the drift ice crashing the lining. When the drift ice thickness is less than 0.9 m , the impact force increases with the drift ice thickness, and the relationship between drift ice size and maximum stress appears linear relationship. When the drift ice thickness is larger than 0.9 m , the impact force changes a little.

In the practical engineering, the two-phase movement between the ice and water is complex which exists multi-factor coupling effects among viscous force, drag force and other factors. The impaction between drift ice and tunnel lining is irregular. It needs further researches in the choice of the impact angle in the simulation.

Acknowledgement

This work was supported by the National Natural Science Foundation of China (No. 51669010, 51969011, 51541902).

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